

# *Electrical Engineering Technology*

## Inductor Introduction

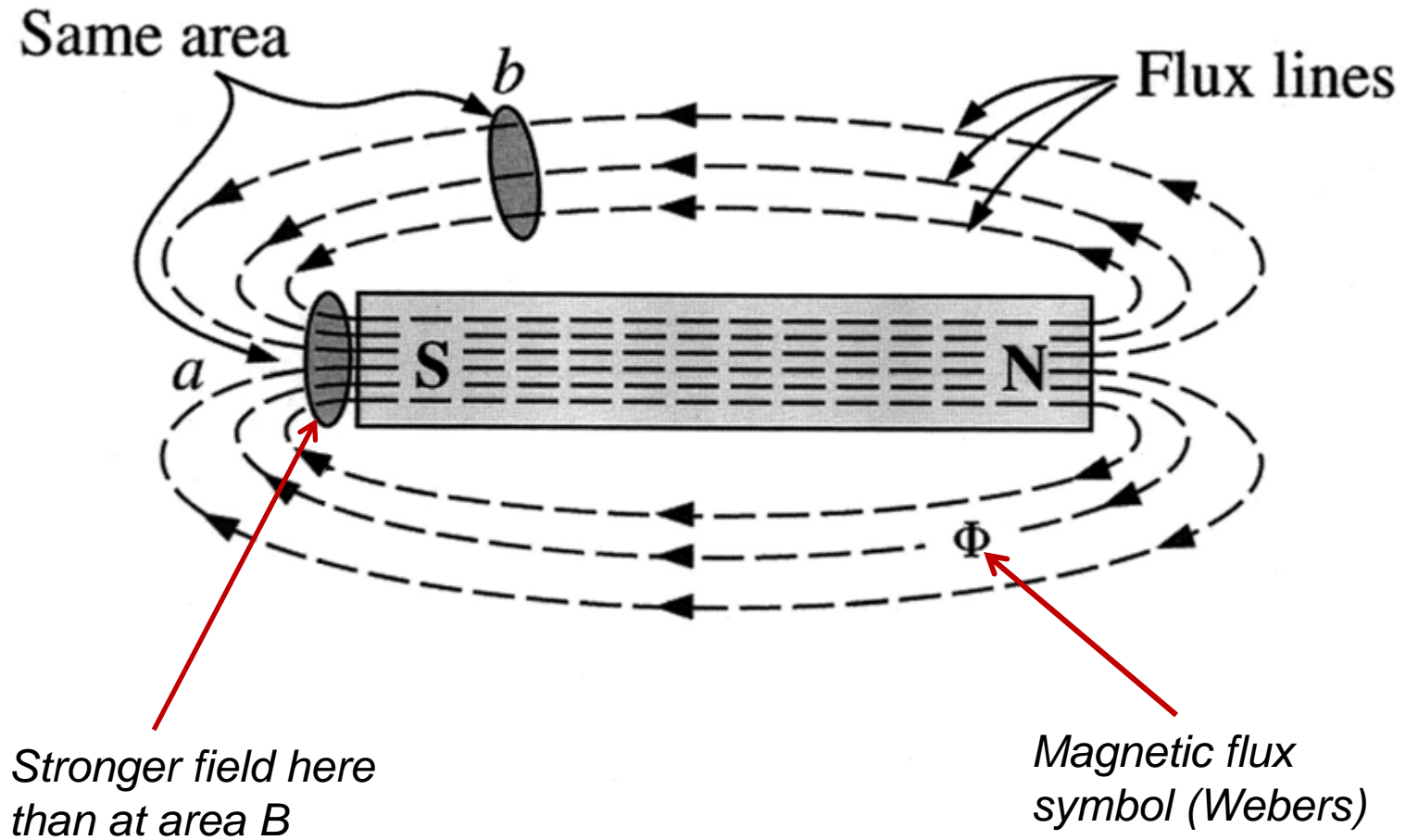
## Inductors vs. Capacitors

- Capacitors store potential energy in an electric field
  - The applied voltage determines total energy stored
  - We can't change the voltage across a capacitor instantly
- Inductors store kinetic energy in a magnetic field
  - The applied current determines the total energy stored
  - We can't change the current through an inductor instantly

## Inductors vs. Capacitors

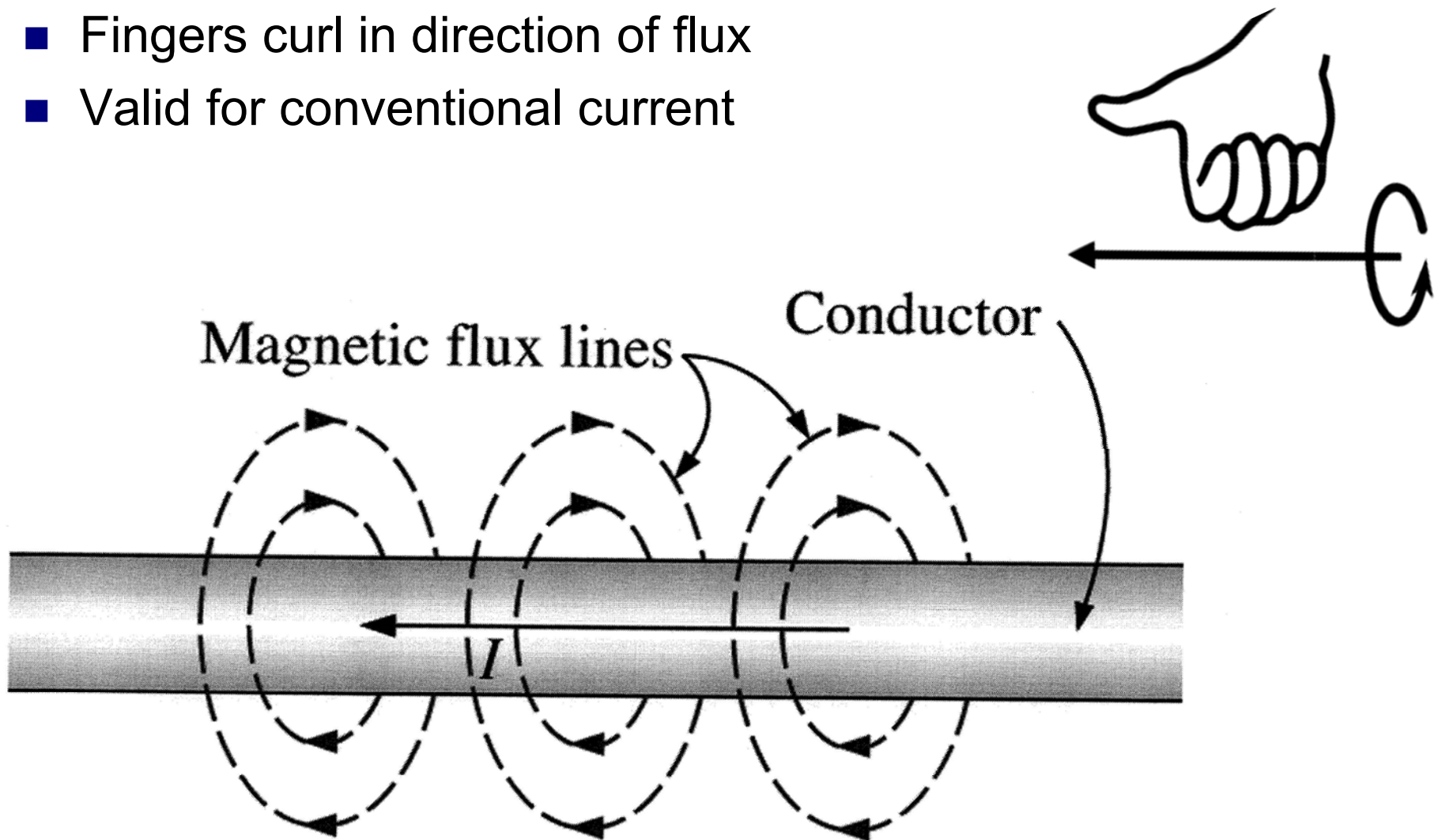
- By definition, you can't "store" kinetic energy, it must remain in motion
- Thus, the current through an inductor must not stop
- If you attempt to stop it instantly, the inductor will generate whatever voltage is necessary to maintain current flow

# Flux

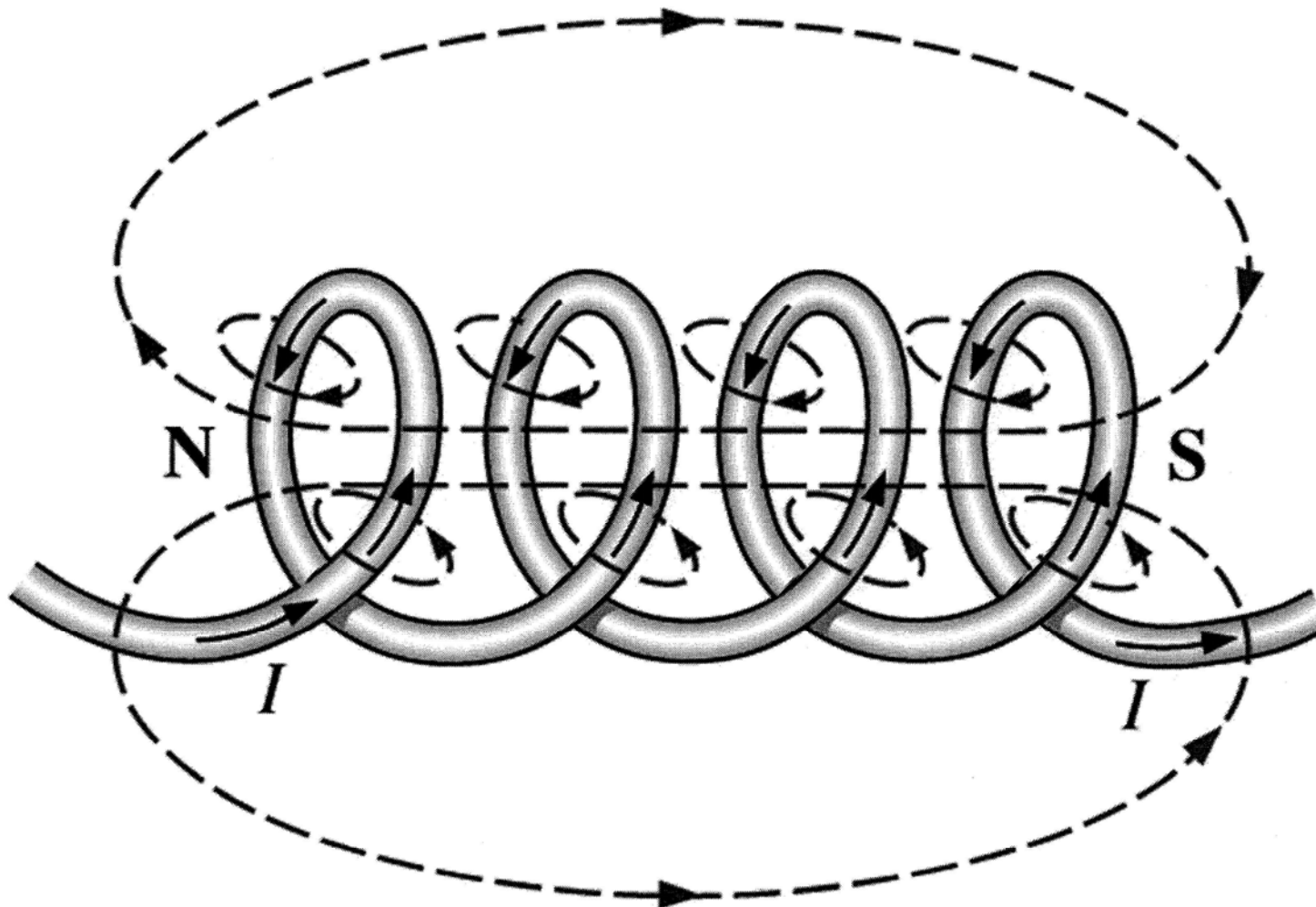


## Right-hand rule

- Thumb points in direction of current flow
- Fingers curl in direction of flux
- Valid for conventional current



## Flux in a coil



# Self-Inductance

- The ability of a coil to oppose any change in current is a measure of self-inductance “L”, measured in Henries (H)

$$H = \frac{Wb}{A} \quad \leftarrow \text{units}$$

$$L = \frac{N^2 \mu A}{l}$$

*N : Number of turns*

*μ : Permeability of the core,  $\mu_0 \bullet \mu_r \frac{Wb}{A \cdot m}$*

*A : Area of the core,  $m^2$*

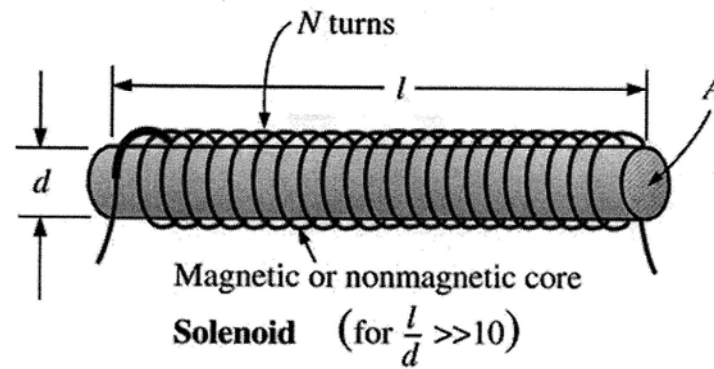
*l : Mean length of the core, m*

*Good low-frequency approximation (DC is 0 frequency)*

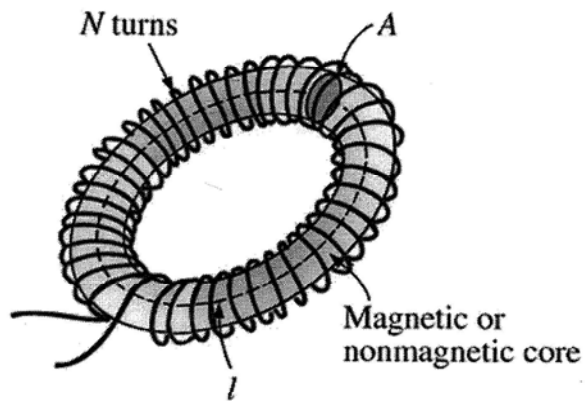
$$L = \mu_r \frac{N^2 \mu_0 A}{l}$$

$$L = \mu_r (L_0) \quad L_0 = \text{Inductance with an air core}$$

# Core shapes



(a)

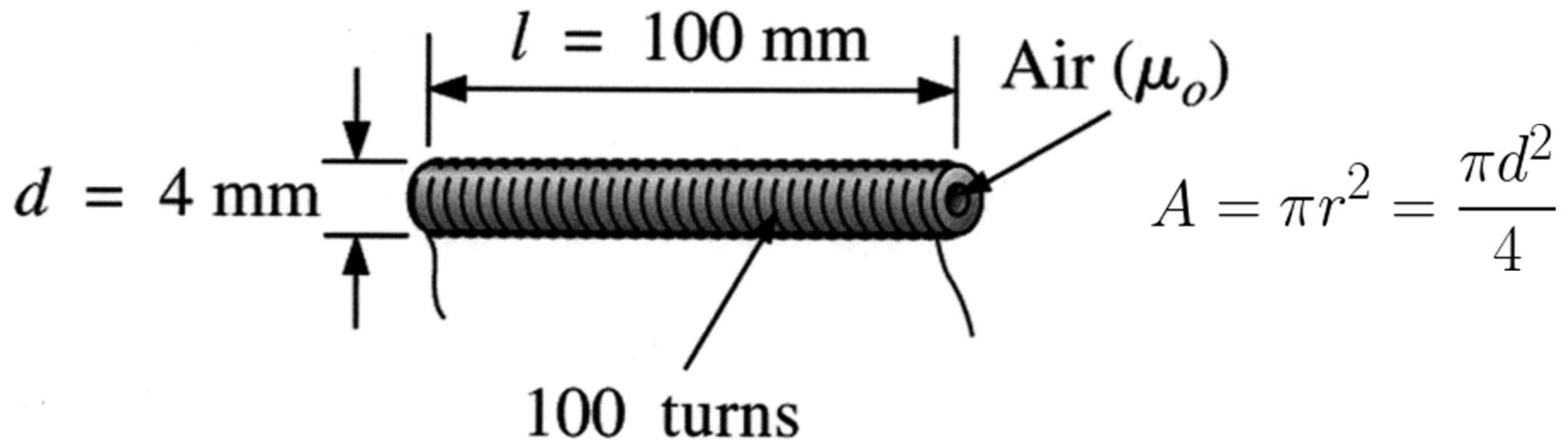


(b)



## Example

- Find L in Henries



$$L = \mu_r L_0$$

$$L_0 = \frac{N^2 \mu_0 A}{l}$$

$$N = 100$$

$$\mu_0 = 4\pi \cdot 10^{-7} \frac{\text{Wb}}{\text{A} \cdot \text{m}}$$

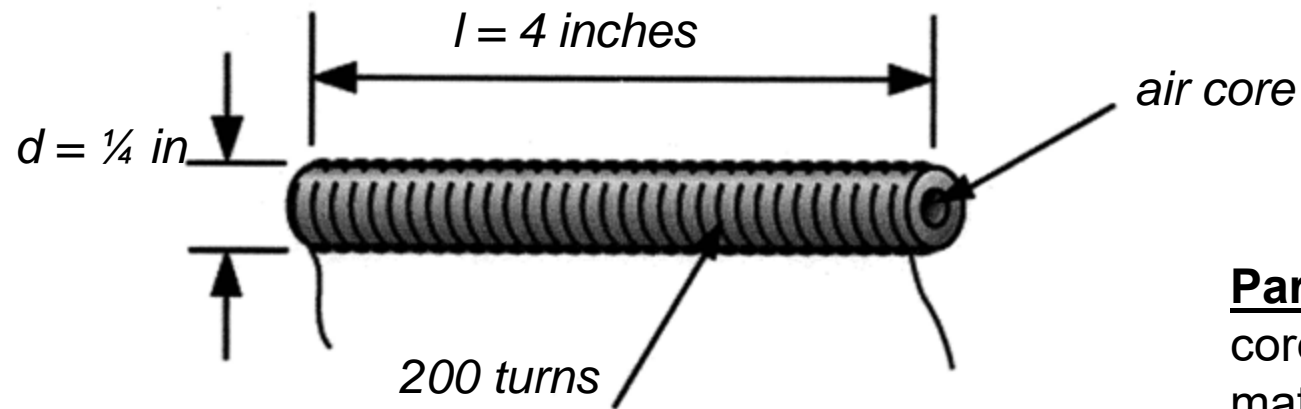
$$A = \frac{\pi d^2}{4} = \frac{\pi (4 \cdot 10^{-3} \text{ m})^2}{4} = 12.57 \cdot 10^{-6} \text{ m}^2$$

$$l = 100 \cdot 10^{-3} \text{ m}$$

$$L_0 = \frac{(100)^2 (4\pi \cdot 10^{-7} \frac{\text{Wb}}{\text{A} \cdot \text{m}}) (12.57 \cdot 10^{-6} \text{ m}^2)}{100 \cdot 10^{-3} \text{ m}} = \boxed{1.58 \mu \text{H}}$$

# ICP

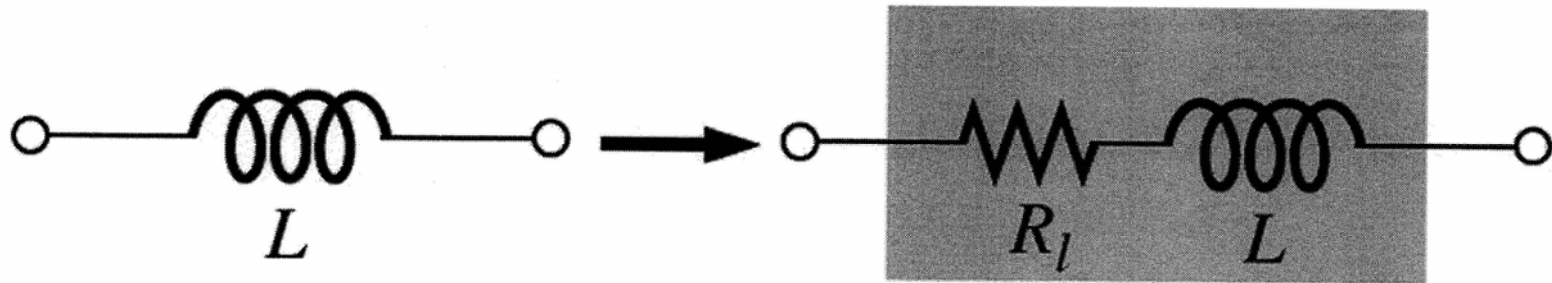
- Find L in Henries



**Part II :** Find L if the core was a magnetic material with  $\mu_r = 125$

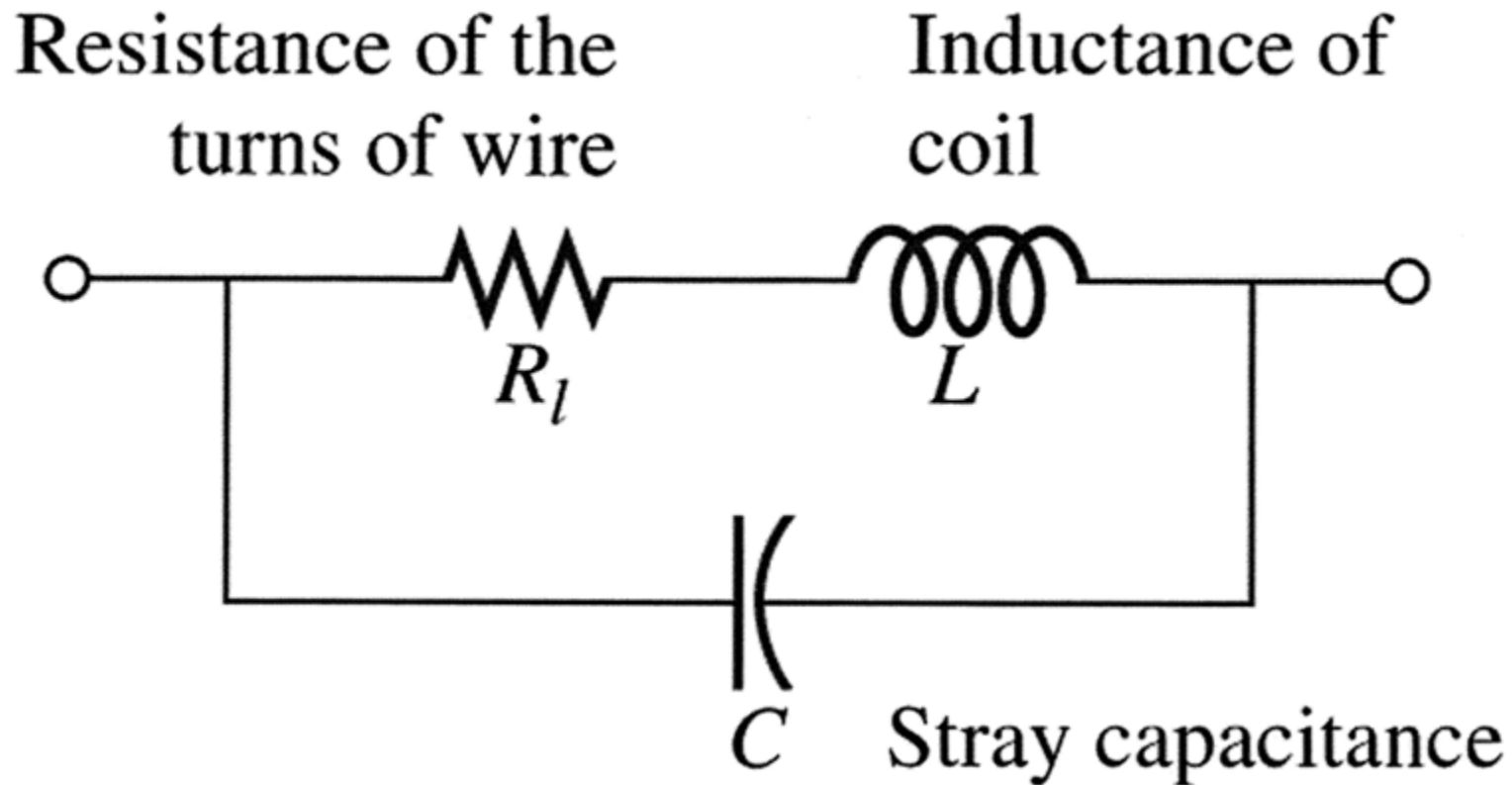
## Practical Model

- Valid for low frequencies

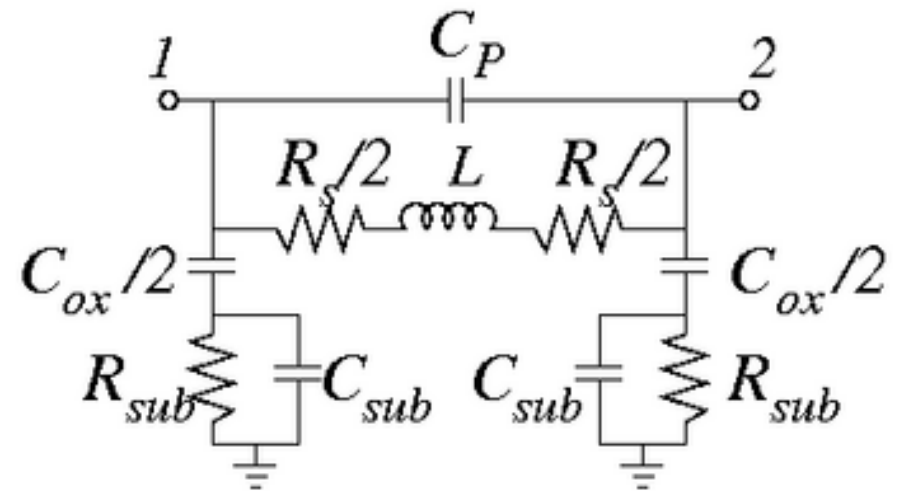
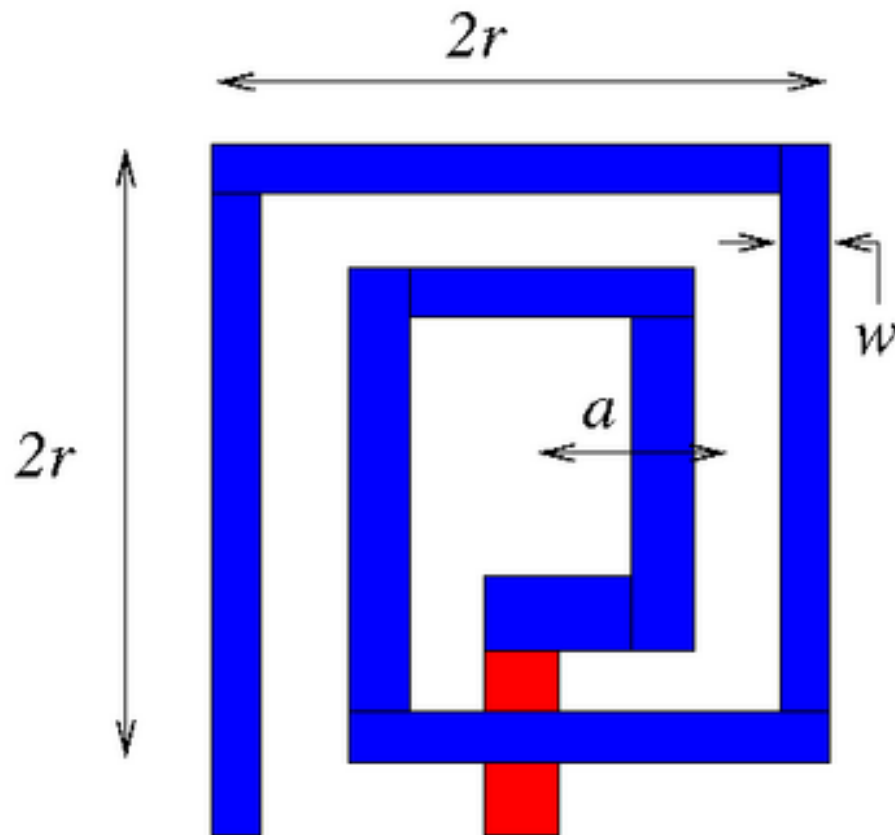


## Practical Model

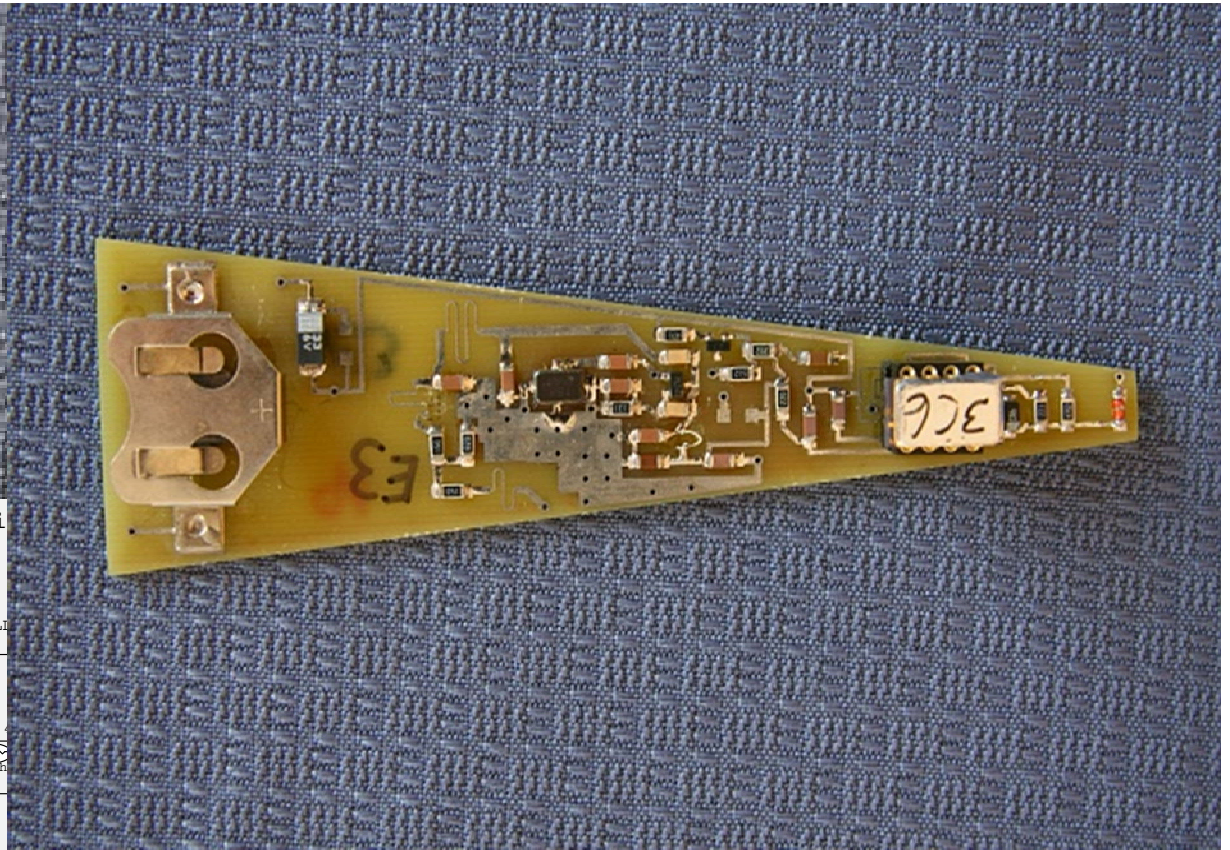
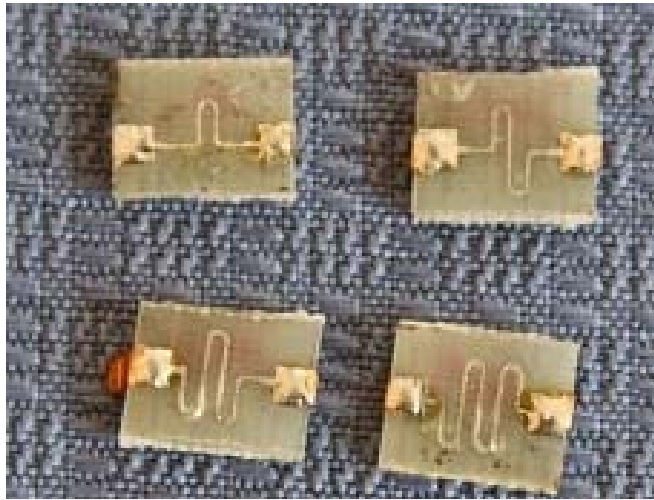
- Slightly better (includes parasitic capacitance)



# Spiral PCB Trace Inductor



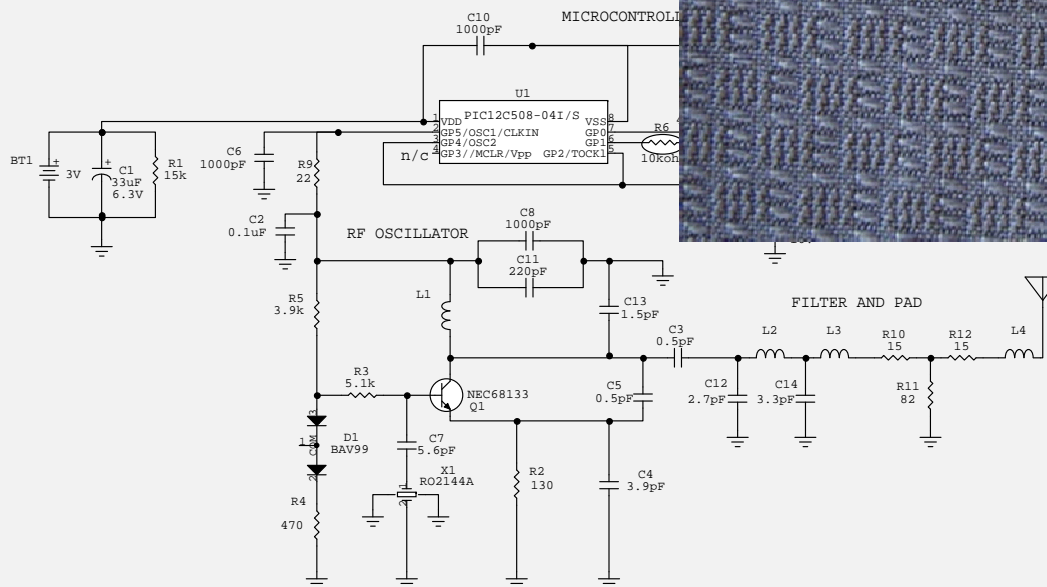
## Example - PCB Trace Inductors



Notes:

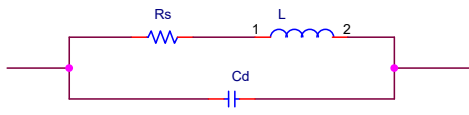
1) L1 through L4 are PWB inductors on 1/16" thick FR-4 substrate

Sensor/Transmi





# MEMS Design – RF Inductors

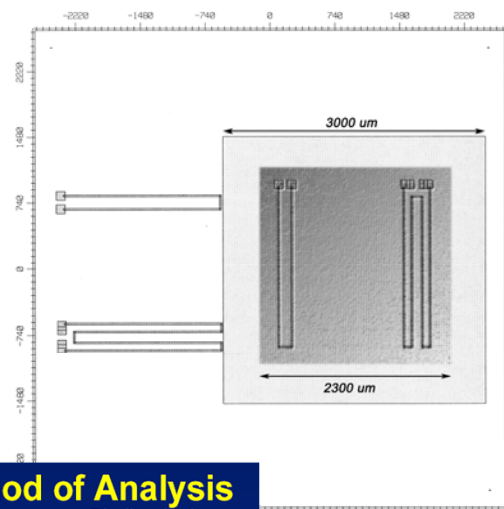


$$Y(j\omega) = j \cdot \omega \cdot Cd + \frac{1}{Rs + j \cdot \omega \cdot L}$$

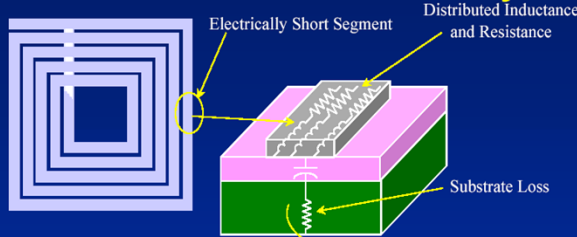
$$Y(j\omega) = \frac{Rs}{Rs^2 + \omega^2 \cdot L^2} + j \cdot \left( \omega \cdot Cd - \frac{\omega \cdot L}{Rs^2 + \omega^2 \cdot L^2} \right)$$

$$\omega_0 = \sqrt{\frac{1}{L \cdot Cd} - \left( \frac{Rs}{L} \right)^2}$$

$$Q \equiv \frac{X}{Rs} \approx \frac{X_L}{Rs} \text{ at low frequencies}$$

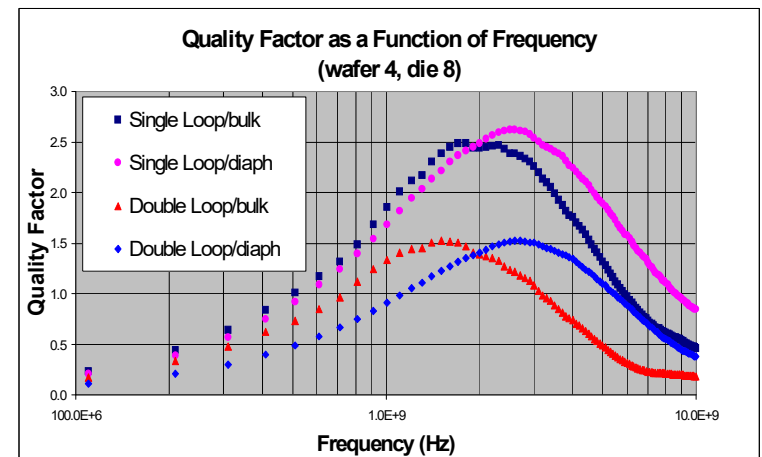
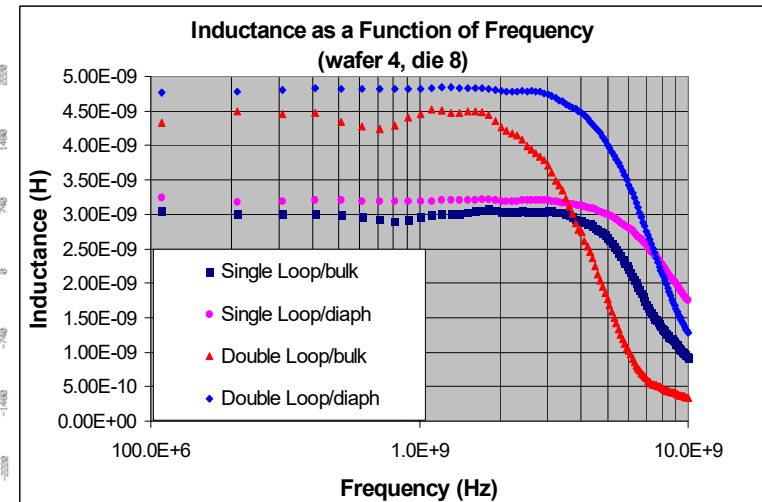


## Efficient/Accurate Method of Analysis



- Model short metal segment as lumped RLC Circuit
- Metal segments are linked capacitively and inductively
- Set up node equations for complete system and solve
- Method equivalent to solving Maxwell's equations

Reference: A. Ruehli, H. Heeb, *MTT*, July '92  
Partial Element Equivalent Circuits (PEEC)



# Schematic Symbols



Air-core



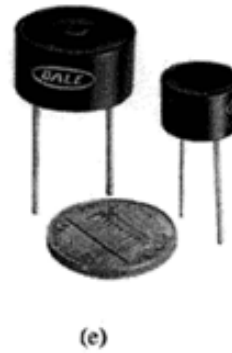
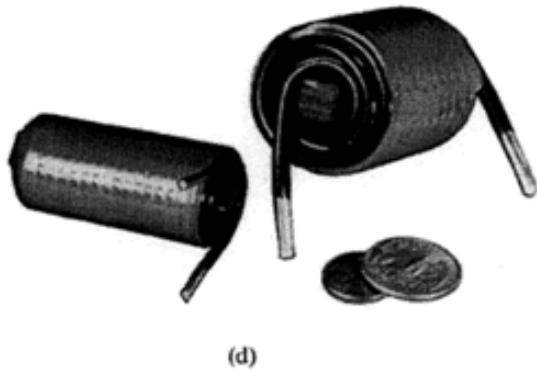
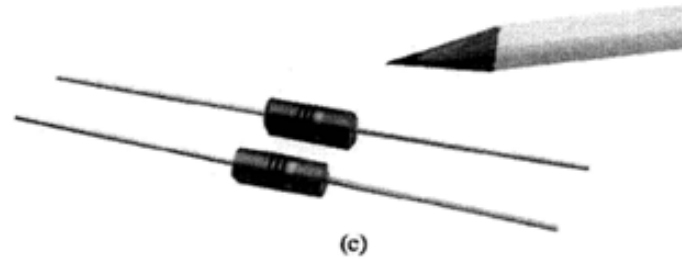
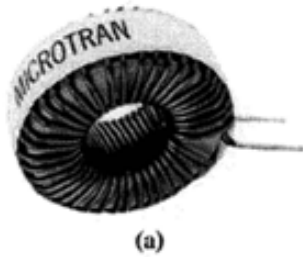
Iron-core



Variable  
(permeability-tuned)

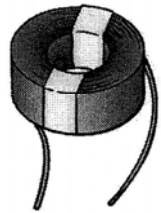


# Types of Inductors



# Types of Inductors/Applications

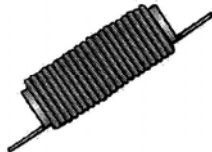
**Type:** Open Core Coil  
**Typical Values:** 3 mH to 40 mH  
**Applications:** Used in low-pass filter circuits. Found in speaker crossover networks.



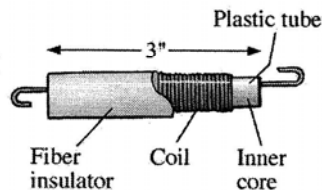
**Type:** Toroid Coil  
**Typical Values:** 1 mH to 30 mH  
**Applications:** Used as a choke in AC power lines circuits to filter transient and reduce EMI interference. This coil is found in many electronic appliances.



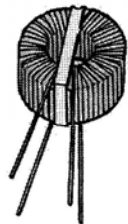
**Type:** Hash Choke Coil  
**Typical Values:** 3  $\mu$ H to 1 mH  
**Applications:** Used in AC supply lines that deliver high currents.



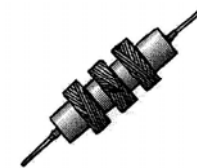
**Type:** Delay Line Coil  
**Typical Values:** 10  $\mu$ H to 50  $\mu$ H  
**Applications:** Used in color televisions to correct for timing differences between the color signal and black and white signal.



**Type:** Common Mode Choke Coil  
**Typical Values:** 0.6 mH to 50 mH  
**Applications:** Used in AC line filters, switching power supplies, battery charges and other electronic equipment.



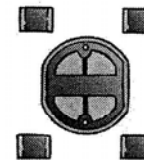
**Type:** RF Chokes  
**Typical Values:** 10  $\mu$ H to 50  $\mu$ H  
**Applications:** Used in radio, television, and communication circuits. Found in AM, FM, and UHF circuits.



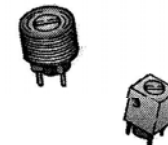
**Type:** Moiled Coils  
**Typical Values:** 0.1  $\mu$ H to 100  $\mu$ H  
**Applications:** Used in a wide variety of circuit such as oscillators, filters, pass-band filters, and others.



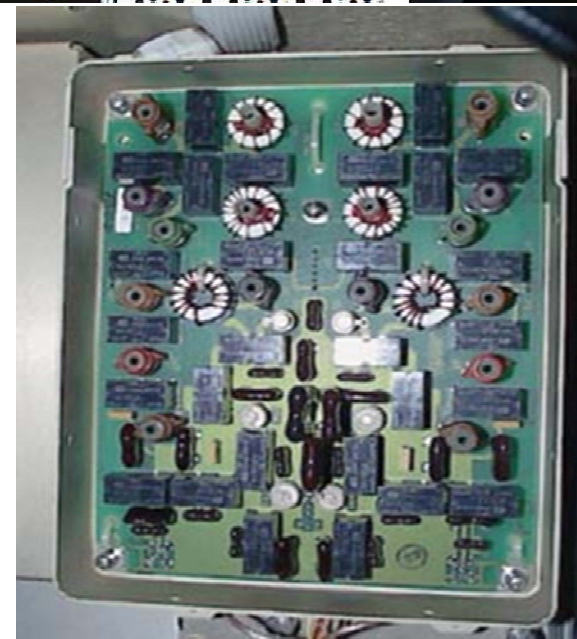
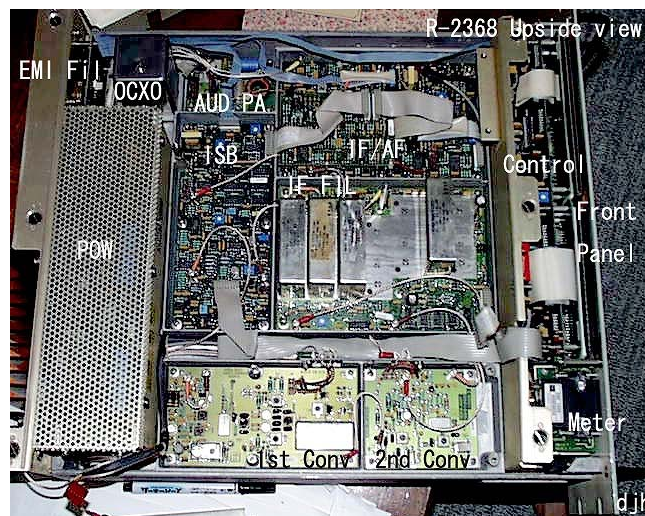
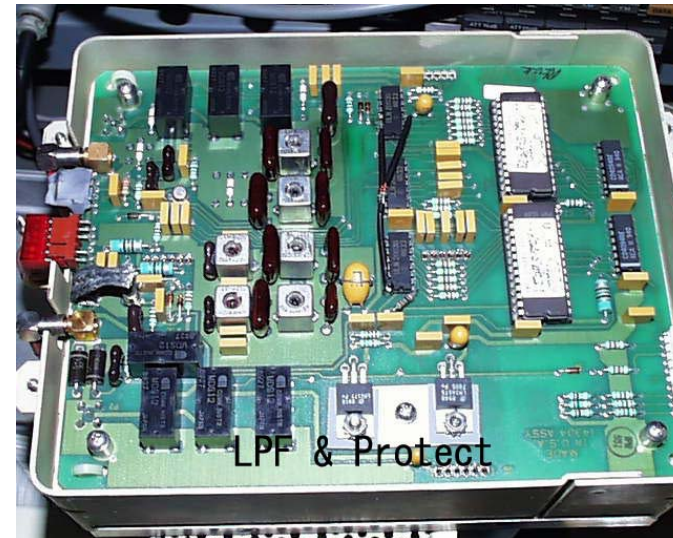
**Type:** Surface Mounted Inductors  
**Typical Values:** 0.01  $\mu$ H to 100  $\mu$ H  
**Applications:** Found in many electronic circuits that require miniature components on multilayered PCB.



**Type:** Adjustable RF Coil  
**Typical Values:** 1  $\mu$ H to 100  $\mu$ H  
**Applications:** Variable inductor used in oscillators and various RF circuits such as CB transceivers, televisions, and radios.



# Through-Hole Inductor Example (RF Filters)





## Surface Mount Inductor Example (RF Filter)

