

The Power Triangle

- Objectives
- Description
- Example with a single load (use your calculator)
 - Find P , S , Q
 - Draw the power triangle
- Multiple loads/branches
 - Approach
 - **In Class Problem**
 - (A) Find P_T (W), Q_T (VARs), S_T (VA)
 - (B) Draw the power triangle
 - (C) Determine F_p
 - (D) Find I_s

The Power Triangle – Objectives

- Become familiar with the differences between average, apparent, and reactive power and how to calculate each for any combination of resistive and reactive elements.
- Become aware of how the real, apparent, and reactive power are related in an ac network and how to find the total value of each for any configuration.
- Understand the concept of power-factor correction and how to apply it to improve the terminal characteristics of a load.

The Power Triangle – Description

- The discussion of power in Chapter 14 included only the average or real power delivered to an ac network.
- We now examine the total power equation in a slightly different form and introduce two additional types of power: apparent and reactive.

$$\text{AVERAGE POWER} \rightarrow P = V_{\text{RMS}} I_{\text{RMS}} \cos(\theta) \quad , (W) \\ \text{DISSIPATED POWER}$$

$$\text{APPARENT POWER} \rightarrow S = V_{\text{RMS}} I_{\text{RMS}} \quad , (V \cdot A)$$

$$\text{REACTIVE POWER} \rightarrow Q = V_{\text{RMS}} I_{\text{RMS}} \sin(\theta) \quad , (VAR)$$

$$\text{RECALL: } \theta = |\theta_V - \theta_I|$$

The Power Triangle – Description

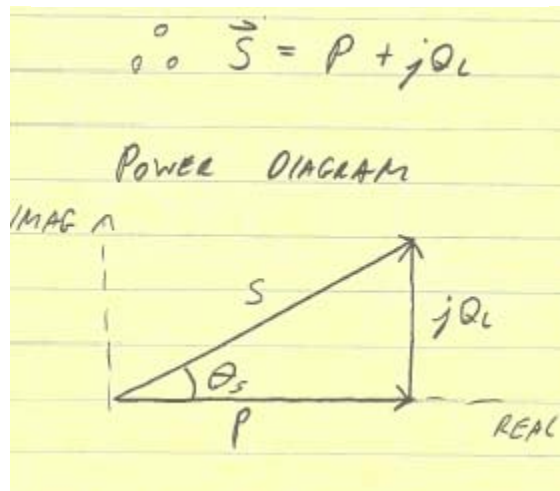
IN THE VECTOR DOMAIN :

$$\vec{S} = \vec{P} + \vec{Q} \quad , \quad \vec{P} = P \angle 0^\circ$$

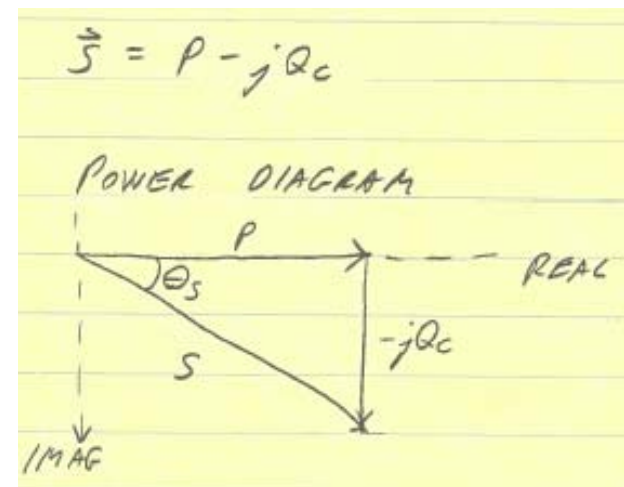
$$\vec{Q} = Q_L \angle 90^\circ \quad - \text{INDUCTIVE}$$

$$Q_C \angle -90^\circ \quad - \text{CAPACITIVE}$$

For **inductive** circuits

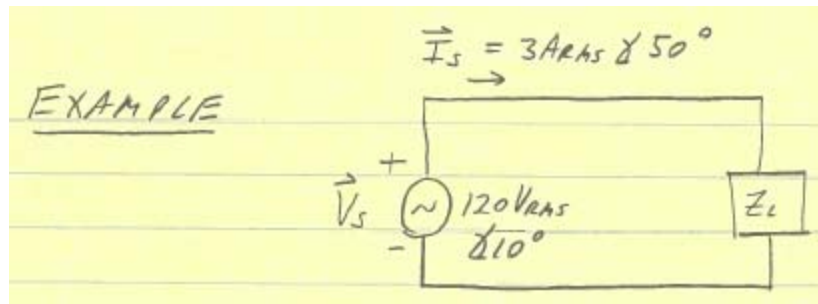


For **capacitive** circuits



The Power Triangle

The Power Triangle – Example (verify the numbers)



FIND : P , THE AVERAGE POWER DELIVERED
 S , " APPARENT POWER
 Q , " REACTIVE POWER
 DRAW THE POWER TRIANGLE

$$P = V_{rms} I_{rms} \cos(\theta)$$

$$= (120V)(3A) \cos(10^\circ - 50^\circ)$$

$$P = (120V)(3A)(0.766) = \boxed{275.8 W}$$

$$S = V_{rms} I_{rms}$$

$$= (120V)(3A) = \boxed{360 VA}$$

$$Q = V_{rms} I_{rms} \sin(\theta)$$

$$= (120V)(3A) \sin(10^\circ - 50^\circ)$$

$$Q = \boxed{231.4 VAR}$$

Is this (C) or (L)? Why?

I leads **V** therefore, capacitive

$$\boxed{231.4 VAR (C)}$$

The Power Triangle – Example (verify the numbers)

$$P = (120V)(3A)(0.766) = \boxed{275.8 \text{ W}}$$

$$S = V_{\text{rms}} I_{\text{rms}} = (120V)(3A) = \boxed{360 \text{ VA}}$$

$$Q = 231.4 \text{ VAR} \Rightarrow \boxed{231.4 \text{ VAR (C)}}$$

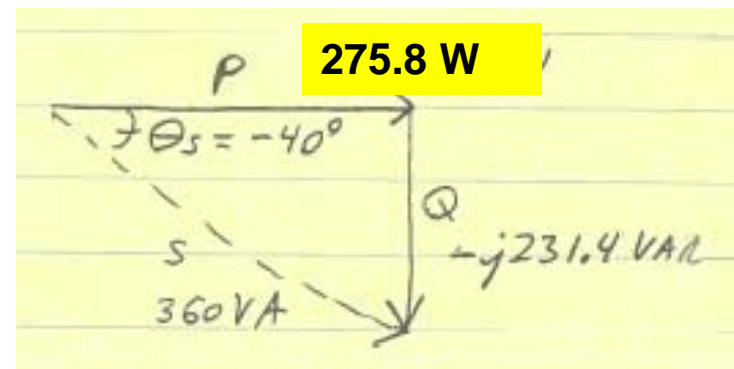
Finding **S**:

$$\text{RECALL: } \vec{S} = \vec{P} + \vec{Q}$$

$$\vec{S} = \underbrace{275.8 \text{ W} \angle 0^\circ}_{\vec{P}} + \underbrace{231.4 \text{ VAR} \angle -90^\circ}_{\vec{Q}} \\ = Q_c \angle -90^\circ$$

$$\boxed{360.02 \text{ VA} \angle -40^\circ} \\ \text{OR} \\ \boxed{275.8 - j231.4} \\ \begin{array}{cc} \uparrow & \uparrow \\ \text{REAL (W)} & \text{REACTIVE (VAR)} \end{array} \\ \text{APPARENT (VA)}$$

Drawing the Power Triangle



The Power Triangle – Approach for multiple loads/branches

1) FIND P , Q FOR EACH CIRCUIT BRANCH

$$2) P_T = P_1 + P_2 + \dots$$

$$3) Q_T = Q_{OT} - Q_{LT}$$

OR

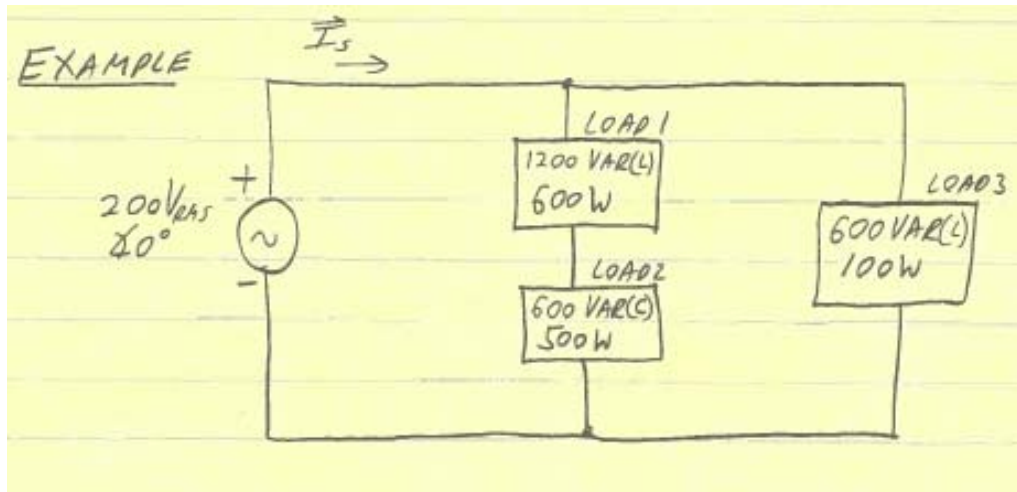
$$Q_{LT} - Q_{CT}$$

OR ADD
" \vec{S} " IN EACH BRANCH
TO FIND \vec{S}_T
(VECTOR FORM)

$$4) S_T = \sqrt{P_T^2 + Q_T^2}$$

$$5) F_p = \frac{P_T}{S_T}, \text{ OR } F_p = \cos(\theta_z) = \cos(\theta_s)$$

In Class Problem



- (A) Find P_T (W), Q_T (VAR), S_T (VA)
- (B) Draw the power triangle
- (C) Determine F_p
- (D) Find I_s

Approach:

- 1) FIND P , Q FOR EACH CIRCUIT BRANCH
 - 2) $P_T = P_1 + P_2 + \dots$
 - 3) $Q_T = Q_{OT} - Q_{LT}$
OR
 $Q_{LT} - Q_{CT}$
 - 4) $S_T = \sqrt{P_T^2 + Q_T^2}$
 - 5) $F_p = P_T / S_T$, OR $F_p = \cos(\theta_z) = \cos(\theta_s)$
- OR ADD
" \vec{S} " IN EACH BRANCH
TO FIND \vec{S}_T
(VECTOR FORM)