

Team Name: _____ Section: _____

Members Present (full names printed):

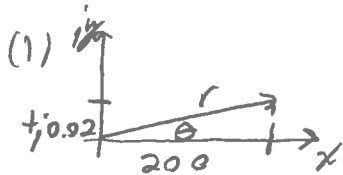
- 1) _____
- 2) _____
- 3) _____
- 4) _____

(I/W STRUCTOR
Sols)

BOX IN YOUR ANSWERS FOR EACH PROBLEM IN THIS HANDOUT

Conversions – Show all your work

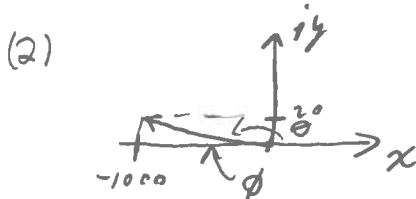
- 1) Convert $200 + j0.02$ to polar form (angle in degrees)
- 2) Convert $-1000 + j20$ to polar form (angle in degrees)
- 3) Convert $6 \angle 40^\circ$ to rectangular form



$$(200)^2 + (0.02)^2 = r^2 \therefore r = 200$$

$$\tan \theta = \frac{y}{x} = \frac{0.02}{200} \therefore \theta = 5.73 \times 10^{-3}^\circ$$

$$200 \angle 5.73 \times 10^{-3}^\circ$$

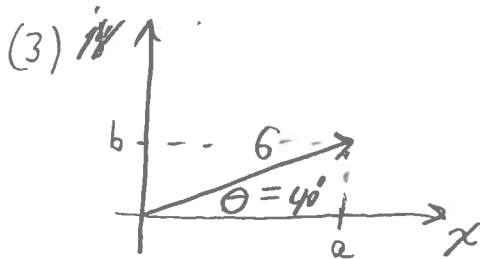


$$(1000)^2 + (20)^2 = r^2 \therefore r = 1,000.2$$

$$\tan(\phi) = \frac{20}{1000} \therefore \phi = 1.146^\circ$$

$$\text{HENCE } \theta = 180^\circ - 1.146^\circ = 178.85^\circ$$

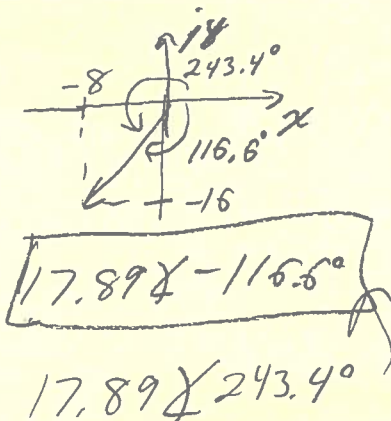
$$1,000 \angle 178.9^\circ$$



$$\cos(\theta) = \frac{a}{6} \therefore a = 6 \cos(40^\circ) = 4.596$$

$$\sin(\theta) = \frac{b}{6} \therefore b = 6 \sin(40^\circ) = 3.857$$

$$\text{OR } 6 \angle 40^\circ = 4.596 + j3.857$$



Conversions – Use your calculator

- 4) Convert $-8 - j16$ to polar form (angle in degrees)
- 5) Convert $2000 \angle -90^\circ$ to rectangular form
- 6) Convert $15 \angle 180^\circ$ to rectangular form

$$17.89 \angle -116.6^\circ$$

$$-j2000$$

$$-15 + j0$$

Addition and Subtraction – Show your work

Solve the following (answers in rectangular form):

7) $(4.2 + j6.8) + (7.6 + j0.2)$

8) $(6.8 - j4.2) - (0.2 + j7.6)$

9) $6\angle 40^\circ - (15 + j0)$

$$\begin{array}{r} (7) \quad 4.2 + j6.8 \\ + \quad 7.6 + j0.2 \\ \hline \boxed{11.8 + j7.0} \end{array}$$

$$\begin{array}{r} (8) \quad (6.8 - j4.2) \\ - \quad (0.2 + j7.6) \\ \hline \boxed{6.6 - j11.8} \end{array}$$

$$\begin{array}{r} (9) \quad 6\angle 40^\circ \rightarrow 4.596 + j3.857 \\ - \quad (15 + j0) \\ \hline \boxed{-10.404 + j3.857} \end{array}$$

Addition and Subtraction – Use your calculator

Solve the following (answers in rectangular form):

10) $10\angle 80^\circ - 12\angle 65^\circ$

11) $(4.2 + j6.8) - (7.6 + j0.2)$

12) $(6.8 + j4.2) + (0.2 + j7.6)$

$$\boxed{-3.33 - j1.03}$$

$$\boxed{-3.4 + j6.6}$$

$$\boxed{7.0 + j11.8}$$

Multiplications and Division – Show your work

Solve the following (answers in polar form, angles in degrees):

13) $(2 + j3)(6 + j8)$

14) $2 \angle 60^\circ / 12 \angle 65^\circ$

15) $(2 + j3)/(6 + j8)$

$$\begin{aligned} (13) (2 + j3)(6 + j8) &= 12 + j16 + j18 + j^2 24 \\ &= 12 + j34 - 24 = -12.0 + j34 \\ &= \boxed{36.06 \angle 109.4^\circ} \end{aligned}$$

$$(14) \frac{2 \angle 60^\circ}{12 \angle 65^\circ} = \frac{2}{12} \angle (60^\circ - 65^\circ) = \frac{1}{6} \angle -5^\circ \approx \boxed{0.166 \angle -5^\circ}$$

$$\begin{aligned} (15) (2 + j3)/(6 + j8) &= \frac{3.606 \angle 56.31^\circ}{10.0 \angle 53.13^\circ} = \frac{3.606}{10.0} \angle 56.31^\circ - 53.13^\circ \\ &= \boxed{360.6 \times 10^{-3} \angle 3.18^\circ} \end{aligned}$$

Multiplications and Division – Use your calculator

Solve the following (answers in polar form, angles in degrees):

16 14) $(3 + j3)(7 + j8) \rightarrow \boxed{45.1 \angle 93.8^\circ}$

17 15) $3 \angle 45^\circ / 1 \angle 5^\circ \rightarrow \boxed{3 \angle 40^\circ}$

18 16) $(2 - j3)/(6 + j2) \rightarrow \boxed{571 \times 10^{-3} \angle -74.7^\circ}$

Conjugation and Problem Solving

19) Find the complex conjugate of $(3 + j4)$

$$\boxed{3 - j4}$$

20) Find the complex conjugate of $3\angle 45^\circ$

$$\boxed{3\angle -45^\circ}$$

21) Find x if: $(5x + j10)(2 - j3) = 90 - j70$

$$\begin{aligned}(5x + j10)(2 - j3) &= 10x - j15x + j20 - j^2 30 \\ &= (10x + 30) + j(-15x + 20) = 90 - j70\end{aligned}$$

$$10x + 30 = 90$$

$$-15x + 20 = -70$$

$$10x = 60$$

$$\text{OR } -15x = -90$$

$$\underline{x = 6}$$

$$\underline{x = 6}$$

$$\therefore \boxed{x = 6}$$

22) Find θ if: $80\angle 0^\circ / 20\angle \theta^\circ = 3.464 - j2 \rightarrow 4\angle -30^\circ$

$$\frac{80\angle 0^\circ}{20\angle \theta^\circ} = 4\angle -30^\circ$$

$$4\angle (0 - \theta)^\circ = +30^\circ$$

$$\therefore \boxed{\theta = +30^\circ}$$