



$$\vec{Z}_1 = 1000 \Omega$$

$$\vec{Z}_{2,3} = (4000 + j6004) \Omega$$

$$\text{KCL} \\ \sum I_{IN} = \sum I_{OUT}$$

$$V_1: 6 \times 10^{-3} \angle 0^\circ = \frac{\vec{V}_1}{\vec{Z}_1} + \vec{I}_x$$

$$\vec{V}_1 \left( \frac{1}{1000} \right) + \vec{I}_x = 6 \times 10^{-3} \angle 0^\circ \quad (1)$$

$$V_2: 0.1 \vec{V}_s + \vec{I}_x = \frac{\vec{V}_2}{\vec{Z}_{2,3}}$$

$$\text{BUT } \vec{V}_s = \vec{V}_1$$

$$\therefore \text{WE HAVE } 0.1 \vec{V}_1 + \vec{I}_x - \frac{\vec{V}_2}{(4000 + j6004)} = 0 \quad (2)$$

$$\text{REARRANGING: } \frac{1}{1000} \vec{V}_1 + 0 \vec{V}_2 + \vec{I}_x = 6 \times 10^{-3} \angle 0^\circ \quad (1)$$

$$0.1 \vec{V}_1 - \frac{\vec{V}_2}{(4000 + j6004)} + \vec{I}_x = 0 \quad (2)$$

ALSO KNOW  $\vec{E}_1 = \vec{V}_2 - \vec{V}_1$

OR  $-\vec{V}_1 + \vec{V}_2 + 0\vec{I}_x = 10\angle 0^\circ \quad (3)$

SOLVE ?

$$1 \times 10^{-3} \vec{V}_1 + 0 \vec{V}_2 + \vec{I}_x = 6 \times 10^{-3} \angle 0^\circ \quad (1)$$

$$0.1 \vec{V}_1 - (138.6 \times 10^6 \angle 56.33^\circ) \vec{V}_2 + \vec{I}_x = 0 \quad (2)$$

$$-\vec{V}_1 + \vec{V}_2 + 0 \vec{I}_x = 10 \angle 0^\circ \quad (3)$$

$$AX = B \quad \therefore X = A^{-1} B$$

$$B = \begin{bmatrix} 54.16 \times 10^{-3} \angle -167.6^\circ \\ 9.947 \angle -66.81 \times 10^{-3}^\circ \\ 6.053 \times 10^{-3} \angle 109.8 \times 10^{-3}^\circ \end{bmatrix} \begin{matrix} \leftarrow \vec{V}_1 \\ \leftarrow \vec{V}_2 \\ \leftarrow \vec{I}_x \end{matrix}$$

$$\vec{I}_{L1} = \frac{\vec{V}_2}{\vec{Z}_{2,3}} = \frac{9.947 V_{rms} \angle -66.81 \times 10^{-3}^\circ}{(4000 + j6004) \Omega}$$

$$\boxed{\vec{I}_{L1} = 1.38 \text{ mA}_{rms} \angle -56.4^\circ}$$

CHECK :  $\vec{E}_1 \stackrel{?}{=} \vec{V}_2 - \vec{V}_1$

$$10 V_{rms} \angle 0^\circ \stackrel{?}{=} (9.947 V_{rms} \angle -66.81 \times 10^{-3}^\circ) - (54.16 \text{ mV}_{rms} \angle -167.6^\circ)$$

$$10 V_{rms} \angle 0^\circ \stackrel{?}{=} 9.99 V_{rms} \angle 179 \times 10^{-6}^\circ$$

YES